

# PHYS 100C Q&A

Thursday, April 09, 2009  
3:21 PM

\* Q: We assume plane waves so that  $\vec{E}$  &  $\vec{B}$  are const for ALL  $x, y$  (if  $\vec{k} \parallel \hat{z}$ ). This is clearly UNPHYSICAL. What about spherical waves?

\* A: Yes, it's UNPHYSICAL (if  $x, y \rightarrow \infty$ ). But most waves can be approximated as plane waves (even spherical ones), as long as curvature of wavefront  $R \gg \lambda$  (wavelength).

Also, see prob. 9.33 in textbook.

\* Q: Whenever we "guess" for a solution (e.g. to Maxwell's Eqs) how do we know it's unique?

\* A: We don't. But! We have showed in Lect. #1 that waves  $f(z, t) = g(z - vt)$  satisfy wave equation, and that Any wave can be expressed as linear combination of sinusoidal functions

$$f(z, t) = \int_{-\infty}^{\infty} \tilde{A}(\vec{k}) e^{i(\vec{k}z - \omega t)}$$

(See Eq. 9.20 & Problem 9.4)

Therefore, our "guess" of harmonic wave  $\sim e^{i(\vec{k}z - \omega t)}$  is much more than a guess, it is instead a general solution describing ANY arbitrary function  $f(z, t)$  that satisfies wave

$f(z,t)$  that satisfies wave equation.

\* Q: In considering boundary conditions we always set boundary at  $z=0$ . How would this change if it's at  $z_0 \neq 0$ ?

\* A: In general expression  $e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)}$  we would get additional term

$k_z \cdot z_0$  in the exponent

Since  $k_z = \frac{\omega}{v} \cdot \sin\theta$ , and  $\theta_I = \theta_R$ ,

these parts are equal for I and R waves.

For T wave:  $\frac{\omega \cdot \sin\theta_T \cdot z_0}{v_2} = \frac{\omega \sin\theta_I \cdot z_0}{v_1}$

since  $\frac{\sin\theta_T}{\sin\theta_I} = \frac{n_1}{n_2} = \frac{v_2}{v_1}$  (Snell's Law)