

## PHYS-100C, Homework #4, due Monday, May 3<sup>rd</sup>.

**Problem 10.1** Show that the differential equations for  $V$  and  $\mathbf{A}$  (Eqs. 10.4 and 10.5) can be written in the more symmetrical form

$$\left. \begin{aligned} \square^2 V + \frac{\partial L}{\partial t} &= -\frac{1}{\epsilon_0} \rho, \\ \square^2 \mathbf{A} - \nabla L &= -\mu_0 \mathbf{J}. \end{aligned} \right\} \quad (10.6)$$

where

$$\square^2 \equiv \nabla^2 - \mu_0 \epsilon_0 \frac{\partial^2}{\partial t^2} \quad \text{and} \quad L \equiv \nabla \cdot \mathbf{A} + \mu_0 \epsilon_0 \frac{\partial V}{\partial t}.$$

**Problem 10.3** Find the fields, and the charge and current distributions, corresponding to

$$V(\mathbf{r}, t) = 0, \quad \mathbf{A}(\mathbf{r}, t) = -\frac{1}{4\pi\epsilon_0} \frac{qt}{r^2} \hat{\mathbf{r}}.$$

**Problem 10.5** Use the gauge function  $\lambda = -(1/4\pi\epsilon_0)(qt/r)$  to transform the potentials in Prob. 10.3, and comment on the result.

**Problem 10.7** In Chapter 5, I showed that it is always possible to pick a vector potential whose divergence is zero (Coulomb gauge). Show that it is always possible to choose  $\nabla \cdot \mathbf{A} = -\mu_0 \epsilon_0 (\partial V / \partial t)$ , as required for the Lorentz gauge, assuming you know how to solve equations of the form 10.16. Is it always possible to pick  $V = 0$ ? How about  $\mathbf{A} = 0$ ?