## GdFe with Au Review

Sebastian Dietze Shpyrko Group Meeting Dec. 17 2012

#### Interaction of linearly polarized light with perpendicular anisotropic magnetic thin films in transmission geometry

$$I = \left| \mathcal{F}\{\tilde{E}(r_{\perp}, z)\} \right|^{2} = |\mathcal{F}\{E_{0}(r_{\perp})\mathcal{C}(r_{\perp})\}|^{2} + |\mathcal{F}\{E_{0}(r_{\perp})M(r_{\perp})\}|^{2}$$

Charge Structure:  $C(r_{\perp}) = e^{-k_0 z_j (r_{\perp}) [B^j + i\Delta^j]}$ 

Magnetic Structure:  $M(r_{\perp}) = -iC(r_{\perp})k_0 z_j (r_{\perp}) [\beta^j + i\delta^j] \widehat{m}_z^j (r_{\perp})$ 



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**Reconstructed Magnetic Structure** 

## Au patterned GdFe layered thin film



# Charge Contrast



$$\frac{I_{wit\,hAU}}{I_{no\,AU}} = 0.9315$$

Off Res: 
$$\frac{I_{wit \, hAU}}{I_{no \, AU}} = 0.989$$
  
On Res:  $\frac{I_{wit \, hAU}}{I_{no \, AU}} = 1.052$ 

## Weak Scattering



No sample (pinhole scattering)

**Off Resonance** 

# **Problem of Weak Scattering**

**Far-Field Diffraction** 



P. Thibault, et al, Ultramicroscopy 109 (2009) 338–343

## Weak Approximation

$$\begin{split} I_{mag} &\cong I_{on} - \frac{\Re\{c_{on}\}}{\Re\{c_{off}\}} e^{-(\mu_{on} - \mu_{off})^{2}} I_{off} + \left(\frac{\Re\{c_{on}\}}{\Re\{c_{off}\}} - 1\right) e^{-\mu_{on}^{2}} I_{WF} \\ c_{on} &= k_{0} \left[ c_{1} (B_{Gd}^{on} + i\Delta_{Gd}^{on}) + c_{2} (B_{Fe}^{off} + i\Delta_{Fe}^{off}) - (B_{Au}^{off} + i\Delta_{Au}^{off}) \right] \\ \mu_{on} &= 2k_{0} \{ c_{1} B_{Gd}^{on} + c_{2} B_{Fe}^{off} \}, B_{Gd}^{on} \gg B_{Fe}^{off} \\ c_{off} &= k_{0} \left[ c_{1} (B_{Gd}^{off} + i\Delta_{Gd}^{off}) + c_{2} (B_{Fe}^{off} + i\Delta_{Fe}^{off}) - (B_{Au}^{off} + i\Delta_{Au}^{off}) \right] \\ \mu_{off} &= 2k_{0} \{ c_{1} B_{Gd}^{off} + c_{2} B_{Fe}^{off} \}, B_{Gd}^{on} \gg B_{Fe}^{off} \\ z_{Gd} (r_{\perp}) &= c_{1} z_{GdFe} (r_{\perp}), z_{Fe} (r_{\perp}) = c_{2} z_{GdFe} (r_{\perp}), c_{1} + c_{2} = 1 \\ z_{Au} (r_{\perp}) + z_{Gd} (r_{\perp}) + z_{Fe} (r_{\perp}) = z \end{split}$$



**Reconstructed Magnetic Structure** 

### Weak Scattering Constraint

$$\tilde{\psi} = \sqrt{\frac{I_m}{I_{WF}}} \widetilde{E_0} e^{i\Delta\theta} \qquad \qquad \alpha = \frac{\zeta_m + I_{WF}}{\sqrt{I * I_{WF}}} = \frac{I_m/|C_0|^2 + I_{WF}}{2\sqrt{I_m * I_{WF}}}$$

$$\cos(\Delta\theta_R - \theta_c)\cosh(\Delta\theta_I) = |C_0|\alpha,$$

 $\sin(\Delta\theta_R - \theta_c)\sinh(\Delta\theta_I) = 0$