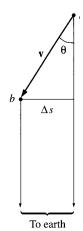
PHYS 100C: Homework #7, due Wed, May 26th



Problem 12.6 Every 2 years, more or less, *The New York Times* publishes an article in which some astronomer claims to have found an object traveling faster than the speed of light. Many of these reports result from a failure to distinguish what is *seen* from what is *observed*—that is, from a failure to account for light travel time. Here's an example: A star is traveling with speed v at an angle θ to the line of sight (Fig. 12.6). What is its apparent speed across the sky?

Problem 12.7 In a laboratory experiment a muon is observed to travel 800 m before disintegrating. A graduate student looks up the lifetime of a muon $(2 \times 10^{-6} \text{ s})$ and concludes that its speed was

$$v = \frac{800 \,\mathrm{m}}{2 \times 10^{-6} \,\mathrm{s}} = 4 \times 10^8 \,\mathrm{m/s}.$$

Figure 12.6

Faster than light! Identify the student's error, and find the actual speed of this muon.

Problem 12.17 Check Eq. 12.29, using Eq. 12.27. [This only proves the invariance of the scalar product for transformations along the x direction. But the scalar product is also invariant under *rotations*, since the first term is not affected at all, and the last three constitute the three-dimensional dot product **a b**. By a suitable rotation, the x direction can be aimed any way you please, so the four-dimensional scalar product is actually invariant under *arbitrary* Lorentz transformations.]

$$-\bar{a}^{0}\bar{b}^{0} + \bar{a}^{1}\bar{b}^{1} + \bar{a}^{2}\bar{b}^{2} + \bar{a}^{3}\bar{b}^{3} = -a^{0}b^{0} + a^{1}b^{1} + a^{2}b^{2} + a^{3}b^{3}.$$
(12.29)

$$\bar{a}^{0} = \gamma (a^{0} - \beta a^{1}),$$

$$\bar{a}^{1} = \gamma (a^{1} - \beta a^{0}),$$

$$\bar{a}^{2} = a^{2},$$

$$\bar{a}^{3} = a^{3}.$$